

$$1. (5x + 2)^2 = (3x - 1)^2 + (4x + 3)^2$$

$$25x^2 + 20x + 4 = 9x^2 - 6x + 1 + 16x^2 + 24x + 9$$

$$25x^2 + 20x + 4 = 25x^2 + 18x + 10$$

$$2x = 6$$

$$x = 3$$

vérification: $17^2 = 8^2 + 15^2$
 $289 = 64 + 225$

$$2. x^2 = 21^2 + 30^2$$

$$x^2 = 1341$$

$$x = \sqrt{1341} \cong 36,61 \dots$$

x mesure 37 cm

3. $\triangle AX Y$ rectangle en A

$$\overline{XY}^2 = 3^2 + 3^2$$

$$\overline{XY}^2 = 18$$

$$\overline{XY} = \sqrt{18} = \sqrt{2 \cdot 3^2} = 3\sqrt{2}$$

$\triangle DF Y$ rectangle en D

$$\overline{FY}^2 = 5^2 + 5^2$$

$$\overline{FY}^2 = 50$$

$$\overline{FY} = \sqrt{50} = \sqrt{2 \cdot 5^2} = 5\sqrt{2}$$

$\triangle GX F$ rectangle en G

$$\overline{XF}^2 = 8^2 + 2^2$$

$$\overline{XF}^2 = 68$$

$$\overline{XF} = \sqrt{68} = \sqrt{2^2 \cdot 17} = 2\sqrt{17}$$

$$\overline{XF}^2 \stackrel{?}{=} \overline{XY}^2 + \overline{FY}^2$$

$$68 = 18 + 50 \text{ donc le triangle } XYF \text{ est rectangle en } Y$$

$$4. \overline{AC} = \sqrt{(3 - (-4))^2 + (-1 - 0)^2} = \sqrt{49 + 1} = \sqrt{50} = \sqrt{2 \cdot 5^2} = 5\sqrt{2}$$